

Instructions

- Complete the problems as if this were an actual test.
 - 70-80 minutes of uninterrupted time. (this means no phones, Netflix, snapchat, etc...I promise you will survive 😊)
 - Don't use your calculator on the NonCalc problems
 - No help from notes, friends, google, etc.
- After you have completed the problems, grade your test using the key provided.
- Try extra problems, similar to the ones you missed, until you feel like you understand those concepts.

Simplify the following. Make sure to show all work.

1. $\tan\theta\cot\theta - \cos^2\theta$

2. $\cos\theta\sec\theta - \frac{\cos\theta}{\sec\theta}$

3. Find the exact value of $\cos 75^\circ$ using a sum or difference identity.4. Find the exact value of $\sin(u+v)$ given that $\sin u = -\frac{15}{17}$ and $\cos v = \frac{5}{13}$.

Both u and v are in Quadrant IV.

5. Use a double-angle formula to find the exact value of $\sin 2u$ when $\cos u = -\frac{12}{13}$, where $\pi < u < \frac{3\pi}{2}$.

6. Use the half-angle identities to find the exact value of $\cos 67.5^\circ$.

Solve the following equations for all values of x .

7. $2\sqrt{2} = -4\cos\theta$

8. $2\cot\theta + \cot^2\theta = -1$

Solve the following equations in the interval $[0, 2\pi)$.

9. $2\sin 3\theta + 1 = 0$

10. $\cos^2\theta + 2 = -3\cos\theta + \sin^2\theta$

Verify the following identities.

$$11. \tan^2 \alpha \sec^2 \alpha + \sec^2 \alpha = \sec^4 \alpha$$

$$12. \frac{\sec \theta \sin \theta}{\tan \theta + \cot \theta} = \sin^2 \theta$$