Non-Calculator.
1)Simplify and state restrictions
a) $\frac{3 x-2}{2 x^{2}}-\frac{4-x}{6}$
b) $\frac{a^{3}-4 a}{a^{2}-2 a-35} \div \frac{a^{2}+4 a+4}{a^{2}-5 a-14}$
c) $\frac{3 x}{2 x-6}+\frac{9}{6-2 x}$
d) $\frac{\frac{1}{x}+3}{\frac{1-9 x^{2}}{4 x}}$
2) Solve for $x$
a) $\frac{6}{x-6}-\frac{2}{x+3}=\frac{18}{x^{2}-3 x-18}$
b) $\frac{1}{2 x}+\frac{3}{x+7}=\frac{-1}{x}$
3) What are the equations of the vertical asymptotes of

$$
f(x)=\frac{1}{x^{2}+2 x-3}
$$

4) Where is the hole in the graph of $f(x)=\frac{(x-3)(x+4)}{(x+1)(x-3)}$ ?
5) Write the equations of the vertical and horizontal asymptotes of $y=\frac{1}{(x+2)^{2}}$
Is the vertical asymptote above odd or even?
6) What is the equation of the horizontal asymptote of $=\frac{2 x}{x-1}$ ?
7)Sketch the graphs completely by finding the domain, holes, VA, $x$-int, $y$-int, EB, and extra points as needed. (Remember end behavior can be HA, SA, or arrows.....you need to figure out what the function has.)
a) $f(x)=\frac{x^{2}-5 x+4}{x^{2}-1}$
b) $f(x)=\frac{2 x^{2}}{x^{2}-4}$
c) $f(x)=\frac{2 x^{2}+7 x+3}{x+1}$
d) $f(x)=\frac{(x-3)^{3}(x+1)}{x^{2}+x-2}$
8)Write a rational function $f$ that has the specified characteristics (there are many correct answers).
VA: $x=-1$
HA: $y=\frac{1}{2}$
hole: $\left(3, \frac{3}{8}\right)$
9)Give the end behavior of the following functions:
a) $g(x)=\frac{(x-4)^{5}(x+2)^{4}}{5 x^{3}-1}$
b) $f(x)=\frac{2 x^{3}-5 x^{2}+7}{x^{2}+x}$
c) $f(x)=\frac{(x-3)^{2}(-x+1)^{4}}{x(x-7)}$
d) $g(x)=\frac{.01 x^{33}-x^{15}}{5-x^{6}}$
7) Simplify.
a) $\frac{1+\frac{2}{x}}{\frac{x^{2}-4}{x^{2}+3 x}}$
b) $\frac{6 x}{x^{2}-2 x-8}-\frac{2}{x+2}+\frac{1}{x-4}$
c) $\frac{x^{2}-2 x-15}{x^{2}-8 x+7} \div \frac{x^{2}+4 x+3}{2 x^{2}-12 x-14}$
8) Solve for $x$.
a) $5(x+4)^{2}-3=32$
b) $5-x^{2}=7 x$
c) $\frac{3}{x+2}=\frac{-1}{x-4}$
9) Graph the following showing at least 2 points
a) $y=-3(x-2)^{2}+3$
b) $y=-\sqrt{x+1}$
10) Graph the rational functional

$$
f(x)=\frac{x^{3}-4 x}{(x+1)(x+2)(x-3)}
$$

## Calculator

14) Sketch a graph that has the following characteristics:

VA: $x=2$ (odd)
VA: $x=-2$ (odd)
SA: $y=x-1$
$y$-int: $(0,2)$
$x$-int: $(1,0)$ (odd)
$x$-int: $(4,0)$ (even)
15)You have to build a corral against an existing fence and you have 100 ft of fencing.

Existing fence

| $x$ |  |
| :---: | :---: |

a) Find the maximum area (include units)
b) What are the dimensions of the corral with the maximum area? (Units!)

